

# KAGRA Type-C suspension simulation

This Jupyter Notebook generates transfer functions of Type-C suspensions of KAGRA.

The simulation code was originally developed by K. Arai for TAMA suspensions.

## Preparation

### Install Wolfram Engine

This notebook is written in Wolfram language (not Python).

In order to run the notebook, you need to install Wolfram Engine from here:

<https://www.wolfram.com/engine/index.ja.php?source=footer>

Then install WolframLanguageForJupyter from here:

<https://github.com/WolframResearch/WolframLanguageForJupyter>

Please follow the instruction there.

### Coordinate system definition



### Load the simulation kernel

Load the core simulation code.

```
In [365]: Get[FileNameJoin[{"dp2D_kernel.3.0.m"}]]
```

### Test Mass Type

There are two variations in Type-C: TM type and PO type. TM type is used for MCE, IMMT1, IMMT2, OMMT1 and OMMT2. PO type is used for MCI, MCo and OSTM1.

In this section, we will compute the TFs of TM type suspensions.

### Load Geometry

```
In [366]: <<"TM_Type_geometry.m"
```

### Find the equilibrium points

```
In [367]: findEquivXY;
findEquivYZ;
findEquivZX;

1: {0, -63.705, 0, 0, 63.5298, 0}
2: {0, -0.00899875, 0, 0, 0.00899875, 0}
```

3: {0,  $-1.9042 \cdot 10^{-10}$ , 0, 0,  $1.9047 \cdot 10^{-10}$ , 0}

## Set the EQOM matrices

In [370]: `setMat`

## Eigen frequencies

In [371]: `Map[MatrixForm, {eigenFreqxy, eigenFreqyz, eigenFreqzx}]`

Out[371]:

$$\left\{ \begin{pmatrix} 0.951544 & 4.53665 \\ 1.47641 & 2.2259 \\ 1.4783 & 3.49672 \\ 1.68502 & 0.582449 \\ 1.93977 & 0.300882 \\ 1.94388 & 0.308963 \\ 3.60058 & 2.50066 \\ 3.62733 & 3.17731 \\ 20.5036 & 17.3268 \end{pmatrix}, \begin{pmatrix} 0.950993 & 4.55488 \\ 1.93931 & 0.300536 \\ 3.5806 & 2.51412 \\ 5.18673 & 3.99282 \\ 6.86533 & 1.27776 \\ 7.11209 & 5.34938 \\ 10.6844 & 8.97122 \\ 23.6514 & 16.6021 \\ 30.88 & 51.3536 \end{pmatrix}, \begin{pmatrix} 0.951448 & 4.53758 \\ 1.65554 & 1.02925 \\ 1.94012 & 0.300623 \\ 3.59292 & 2.50926 \\ 5.18673 & 3.99282 \\ 6.86533 & 1.27776 \\ 7.94257 & 5.07256 \\ 14.794 & 12.9182 \\ 23.6514 & 16.6021 \end{pmatrix} \right\}$$

## Calculate vibration isolation ratio

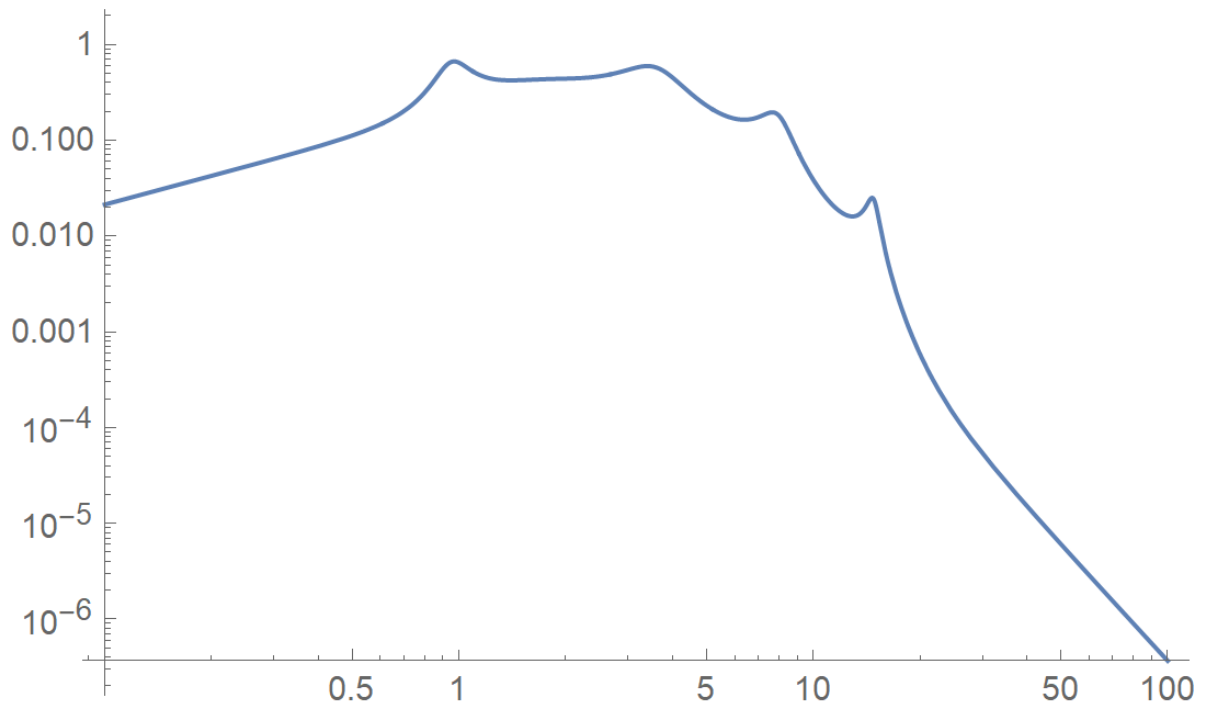
In [372]: `calcVIRxy;`  
`calcVIRyz;`  
`calcVIRzx;`

iso{X|Y|Zeta}{X|Y|Zeta}{IFM}xy have been set.  
 iso{Y|Z|Xi}{Y|Z|Xi}{IFM}yz have been set.  
 iso{Z|X|Eta}{Z|X|Eta}{IFM}zx have been set.

### Plot vibration isolation ratio for Pitch

In [375]: `LogLogPlot[Abs[isoXEtaFzx], {f, 0.1, 100}]`

Out[375]:



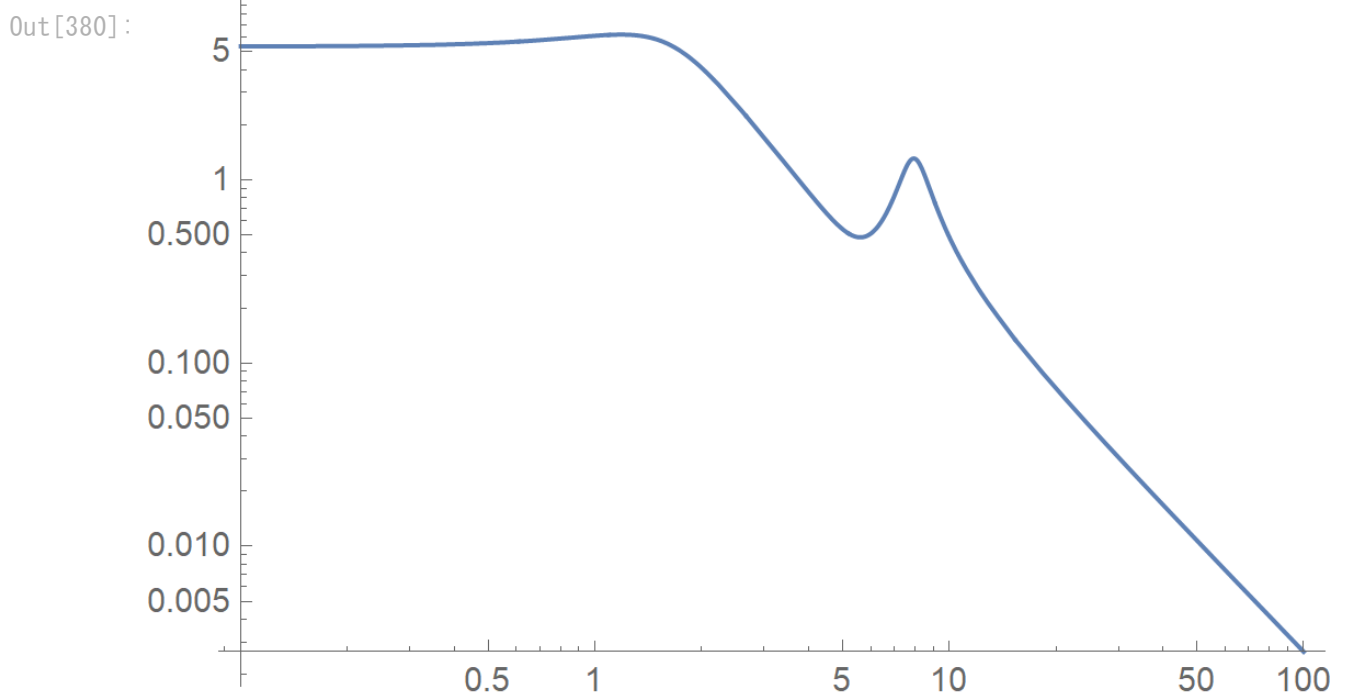
## Calculate actuation transfer functions

```
In [377]: calcActxy;
          calcActyz;
          calcActzx;
```

```
act{X|Y|Zeta}{X|Y|Zeta}{IFM}xy have been set.
act{Y|Z|Xi}{Y|Z|Xi}{IFM}yz have been set.
act{Z|X|Eta}{Z|X|Eta}{IFM}zx have been set.
```

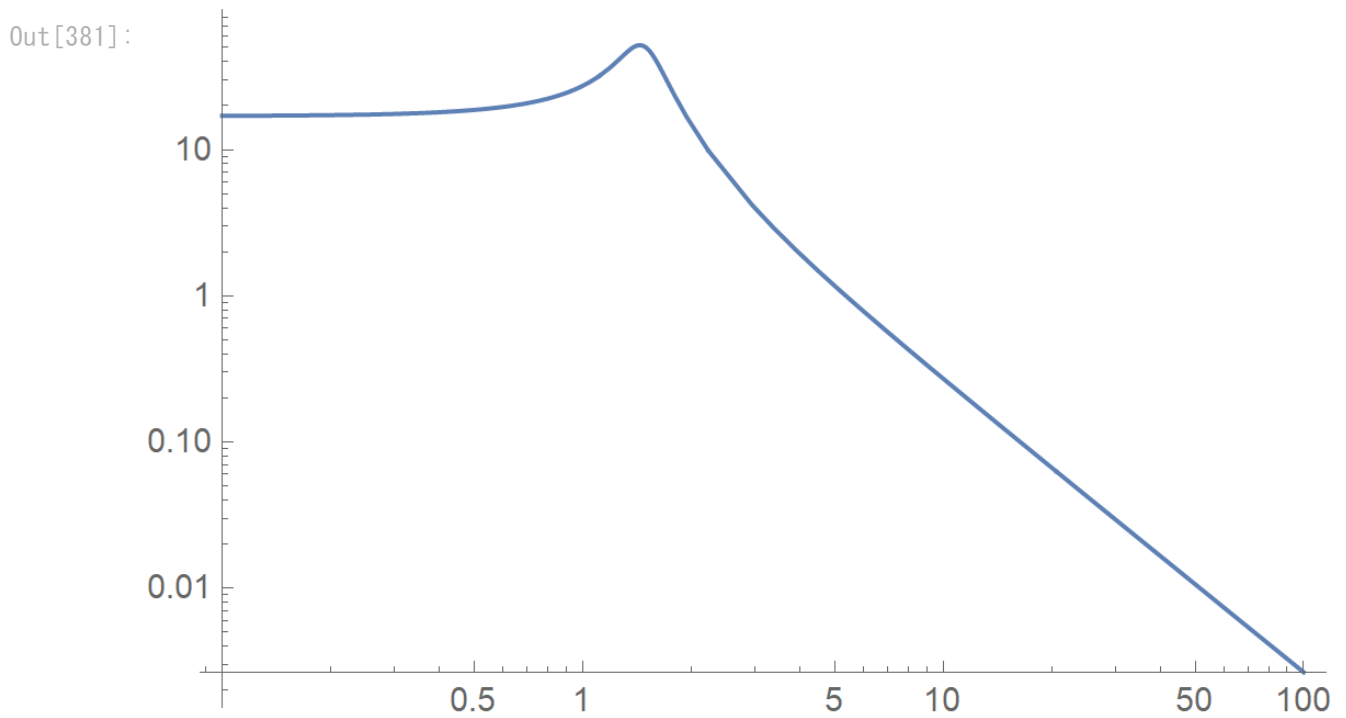
## Actuation TF: Pitch -> Pitch

```
In [380]: LogLogPlot[Abs[actEtaEtaFzx], {f, 0.1, 100}]
```



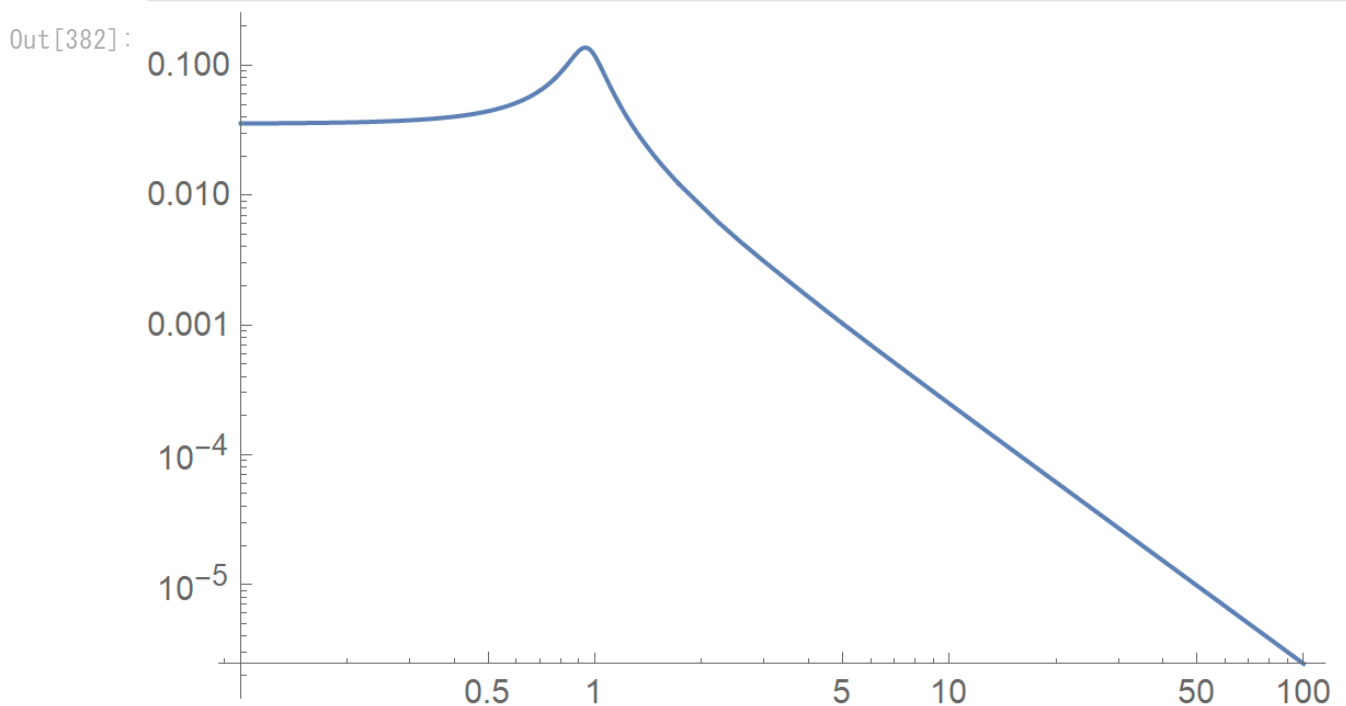
## Actuation TF: Yaw -> Yaw

```
In [381]: LogLogPlot[Abs[actZetaZetaFxy], {f, 0.1, 100}]
```



## Actuation TF: L -> L

```
In [382]: LogLogPlot[Abs[actXXFxy], {f, 0.1, 100}]
```



## Save data

```
In [383]: fisoXXF[f_] = Abs[isoXXFzx];
fisoYYF[f_] = Abs[isoYYFyz];
fisoZZF[f_] = Abs[isoZZFzx];
fisoXEtaF[f_] = Abs[isoXEtaFzx];
fisoZEtaF[f_] = Abs[isoZEtaFzx];
```

```

writeIgor["Type-C_TM_Isolation.dat",
{"#freq", "XX", "YY", "ZZ", "X->Pitch"},
{freq, fisoXXF[freq], fisoYYF[freq], fisoZZF[freq], fisoXEtaF[freq]}
];

factXXF[f_]=Abs[actXXFzx];
factXXFAng[f_]=Arg[actXXFzx]/Pi*180;

factEtaEtaF[f_]=Abs[actEtaEtaFzx];
factEtaEtaFAng[f_]=Arg[actEtaEtaFzx]/Pi*180;
factZetaZetaF[f_]=Abs[actZetaZetaFxy];
factZetaZetaFAng[f_]=Arg[actZetaZetaFxy]/Pi*180;

writeIgor["Type-C_TM_Act.dat",
{"#freq", "Abs:Len", "Phase:Len", "Abs:Pit", "Phase:Pit", "Abs:Yaw", "Phase:Yaw"},
{freq, factXXF[freq], factXXFAng[freq], factEtaEtaF[freq], factEtaEtaFAng[freq], factZetaZetaF[freq], factZetaZetaFAng[freq]}
];

```

## Pick-off Type

In this section, we will compute the TFs of PO type suspensions.

## Load Geometry

In [396]: `<<"PO_Type_geometry.m"`

## Find the equilibrium points

In [397]:

```

findEquivXY;
findEquivYZ;
findEquivZX;

1: {0, 18.3526, 0, 0, -21.3772, 0}
2: {0, -0.00862611, 0, 0, 0.00862611, 0}
3: {0, -1.37646 10-9, 0, 0, 1.37648 10-9, 0}

```

## Set the EQOM matrices

In [400]: `setMat`

## Eigen frequencies

In [401]: `Map[MatrixForm, {eigenFreqxy, eigenFreqyz, eigenFreqzx}]`

Out[401]:

$$\left\{ \begin{pmatrix} 0.96447 & 4.87219 \\ 1.28209 & 0.403662 \\ 1.55938 & 1.17266 \\ 1.67453 & 0.322864 \\ 2.17403 & 2.21149 \\ 3.99642 & 1.19615 \\ 4.02243 & 2.8971 \\ 6.12656 & 23.9612 \\ 11.8006 & 11.9933 \end{pmatrix}, \begin{pmatrix} 0.957211 & 5.00847 \\ 1.664 & 0.324476 \\ 4.01987 & 2.84166 \\ 6.54159 & 15.174 \\ 6.92227 & 1.42326 \\ 7.18528 & 4.14944 \\ 13.6283 & 2.49809 \\ 32.3155 & 21.8628 \\ 37.3849 & 299.515 \end{pmatrix}, \begin{pmatrix} 0.964389 & 4.87216 \\ 1.67453 & 0.322863 \\ 2.00268 & 2.51254 \\ 4.02243 & 2.8971 \\ 6.54159 & 15.174 \\ 6.92227 & 1.42326 \\ 10.0261 & 11.0494 \\ 11.0922 & 34.0537 \\ 32.3155 & 21.8628 \end{pmatrix} \right\}$$

## Calculate vibration isolation ratio

In [402]:

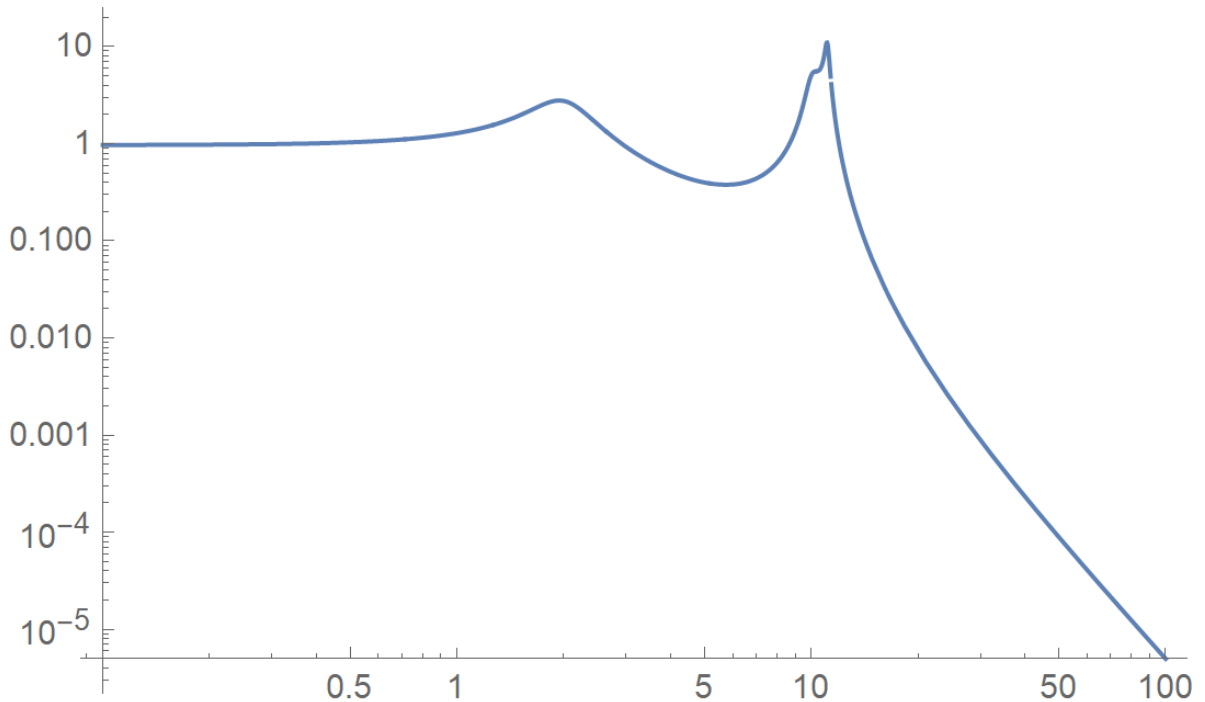
```
calcVIRxy;
calcVIRyz;
calcVIRzx;
```

iso{X|Y|Zeta}{X|Y|Zeta}{IFM}xy have been set.  
 iso{Y|Z|Xi}{Y|Z|Xi}{IFM}yz have been set.  
 iso{Z|X|Eta}{Z|X|Eta}{IFM}zx have been set.

In [405]:

```
LogLogPlot[Abs[isoEtaEtaFzx], {f, 0.1, 100}]
```

Out[405]:



## Calculate actuation transfer functions

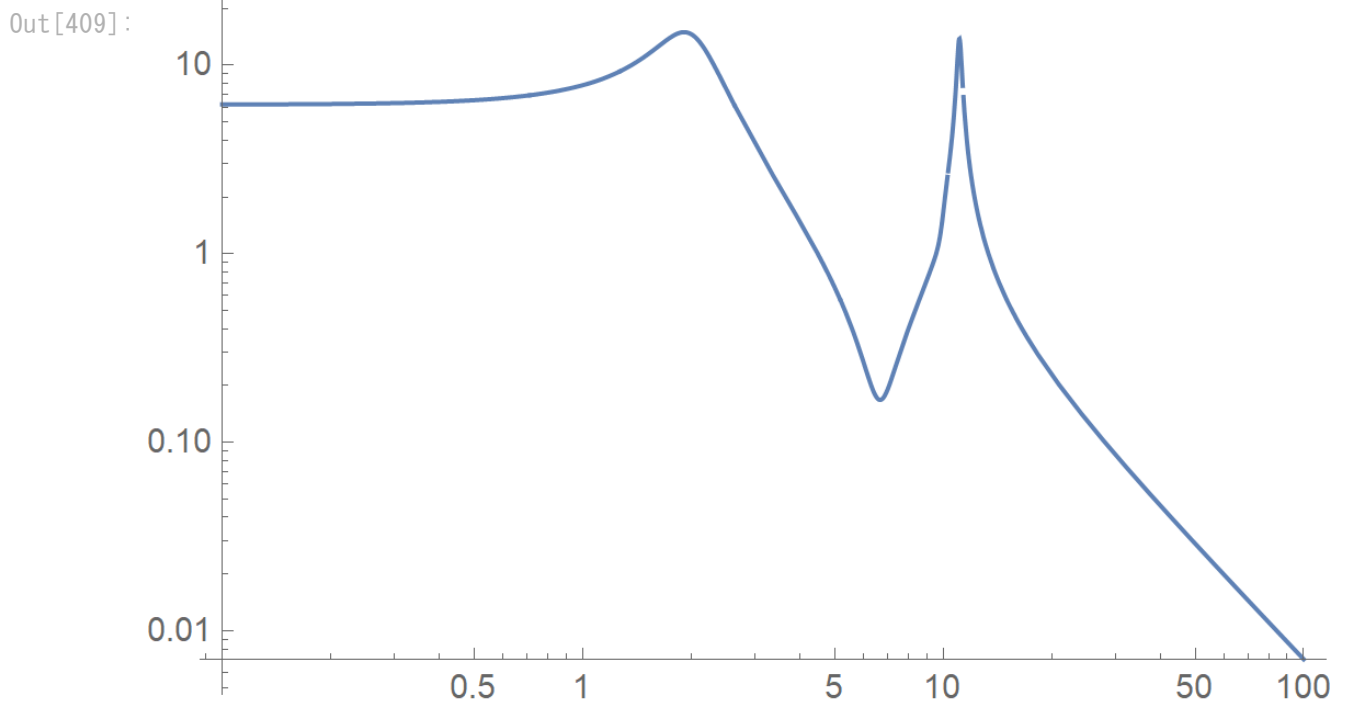
In [406]:

```
calcActxy;
calcActyz;
calcActzx;
```

act{X|Y|Zeta}{X|Y|Zeta}{IFM}xy have been set.  
 act{Y|Z|Xi}{Y|Z|Xi}{IFM}yz have been set.  
 act{Z|X|Eta}{Z|X|Eta}{IFM}zx have been set.

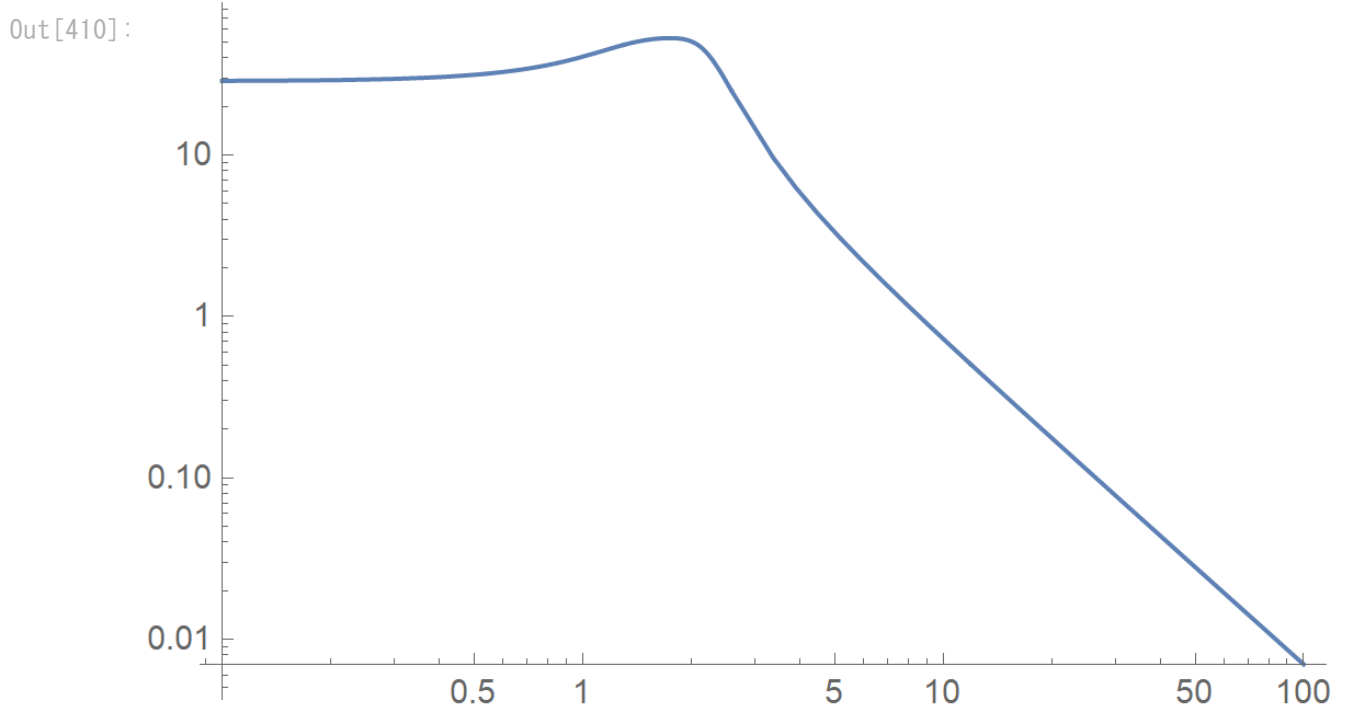
## Actuation TF: Pitch -> Pitch

```
In [409]: LogLogPlot[Abs[actEtaEtaFzx], {f, 0.1, 100}]
```



### Actuation TF: Yaw -> Yaw

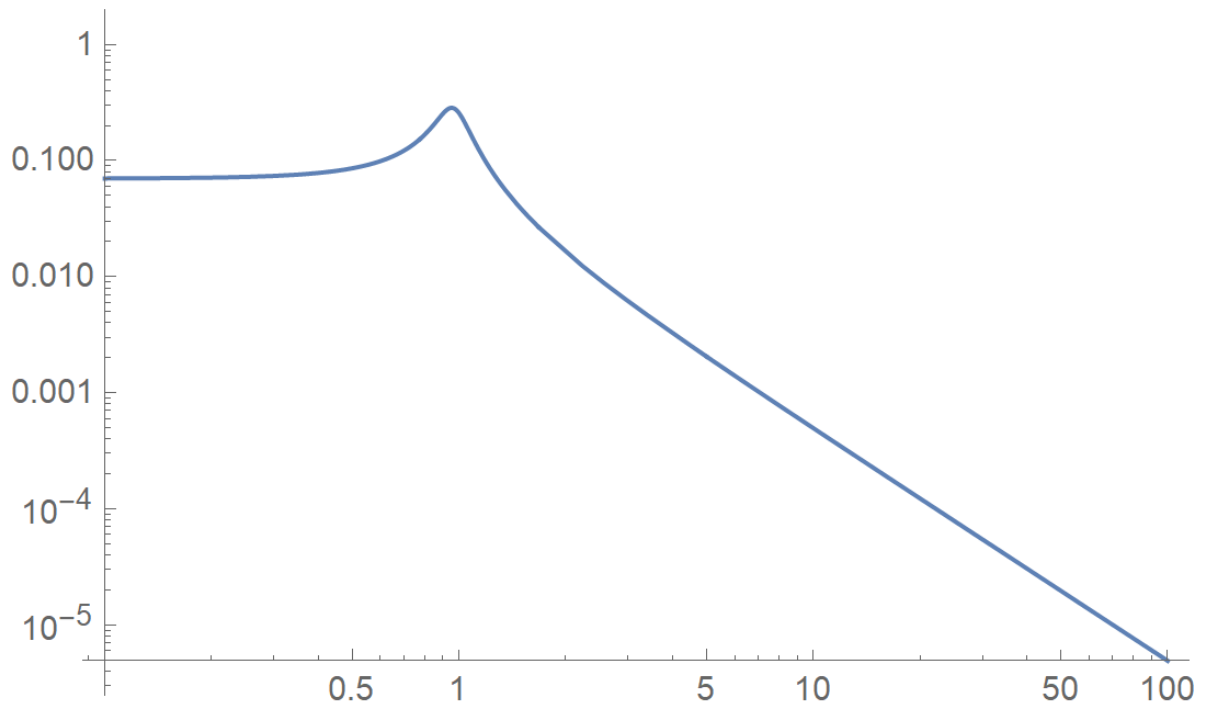
```
In [410]: LogLogPlot[Abs[actZetaZetaFxy], {f, 0.1, 100}]
```



### Actuation TF: L -> L

```
In [411]: LogLogPlot[Abs[actXXFxy], {f, 0.1, 100}]
```

Out[411]:



In [426]: `vecActXxy`

Out[426]: {0, 0, 0, 1, 0, 0, 0, 0, 0}

## Save data

```
In [412]:
fisoXXF[f_]=Abs[isoXXFzx];
fisoYYF[f_]=Abs[isoYYFyz];
fisoZZF[f_]=Abs[isoZZFzx];
fisoXEtaF[f_]=Abs[isoXEtaFzx];

writeIgor["Type-C_P0_Isolation.dat",
{"#freq","XX","YY","ZZ","X->Pitch"},
{freq, fisoXXF[freq], fisoYYF[freq], fisoZZF[freq], fisoXEtaF[freq]}
];

factXXF[f_]=Abs[actXXFzx];
factXXFang[f_]=Arg[actXXFzx]/Pi*180;

factEtaEtaF[f_]=Abs[actEtaEtaFzx];
factEtaEtaFang[f_]=Arg[actEtaEtaFzx]/Pi*180;
factZetaZetaF[f_]=Abs[actZetaZetaFxy];
factZetaZetaFang[f_]=Arg[actZetaZetaFxy]/Pi*180;

writeIgor["Type-C_P0_Act.dat",
{"#freq","Abs:Len","Phase:Len","Abs:Pit","Phase:Pit","Abs:Yaw","Phase:Yaw"},
{freq, factXXF[freq], factXXFang[freq], factEtaEtaF[freq], factEtaEtaFang[freq], factZetaZetaF[freq], factZetaZetaFang[freq]}
];
```

In [ ]: